

**A sampling distribution (for the mean) is a frequency distribution created by using the mean of repeated samples as data points for the distribution**

**Two important properties of a sampling distribution for the mean are**

$$1. \mu_{\bar{x}} = \mu$$

$$2. \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

**Suppose random samples are chosen from a population that has an unknown distribution, but has a known mean and standard deviation**

- 1. If samples of size  $n > 30$  are drawn then the sampling distribution of sample means will form a normal distribution**
- 2. If the original population is approximately normal, then samples of any size will form a normal distribution**

To calculate normal probabilities related to a sample mean of  $n$  items, rather than a single item, we can use the same `normcdf` function in the calculator with 4 inputs, but the last input needs to be  $\sigma/\sqrt{n}$ .

`normcdf(lower  $\bar{x}$ , upper  $\bar{x}$ ,  $\mu$ ,  $\sqrt{\sigma^2/n}$ )`

**2 The average age of a vehicle registered in the United States is 96 months (8 years). Assume the standard deviation to be 16 months. If a random sample of 36 cars is selected, find the probability that the mean age of the sample is between 90 and 100 months**

**3 According to Runner's World magazine, the finishing times of all the 10K races they have tracked in the last 10 years are normally distributed with a mean of 61 minutes and a standard deviation of 9 minutes. If samples of 12 runners are taken, what percentage of mean finishing times will be below 58 minutes?**

**4 According to the U.S. Department of Agriculture, the mean daily calorie intake of males aged 20 to 39 years old is 2716 calories with a standard deviation of 728 calories. Assuming the distribution of calorie intake forms a normal distribution, what is the probability that a mean of a random sample of 25 males is 2750 calories and higher?**